3-dimensional Rossby vortices Structure and evolution of

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Instabilities and Structures in Proto-Planetary disks Workshop Marseille 2012





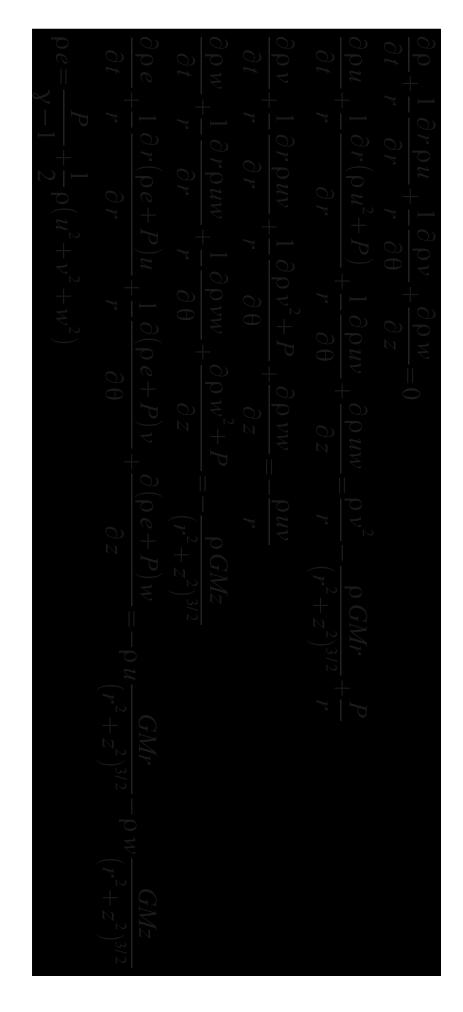
Summary

- The system of equations
- Vortex formation by Rossby Wave Instability
- Long term evolution

3D structure of the resulting vortex

Conclusion

The system of equations

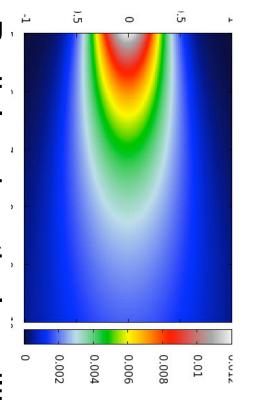


developed for disk studies (Inaba et al, 2001); it is parallelized to permit MUSCL-Hancock scheme. The code is based on a 2D version specifically Solved numerically with a finite volume method using a second order long and high resolution runs

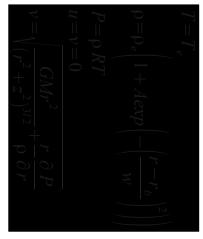
Initial condition

Stable equilibrium state

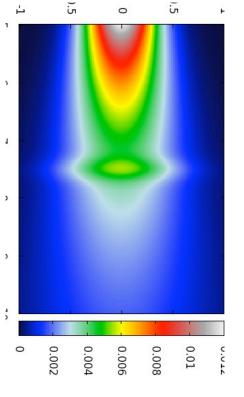




Perturbed equilibriium state



+ noise



gravity and pressure gradient are satisfied Radial and vertical equilibrium between centrifugal force,

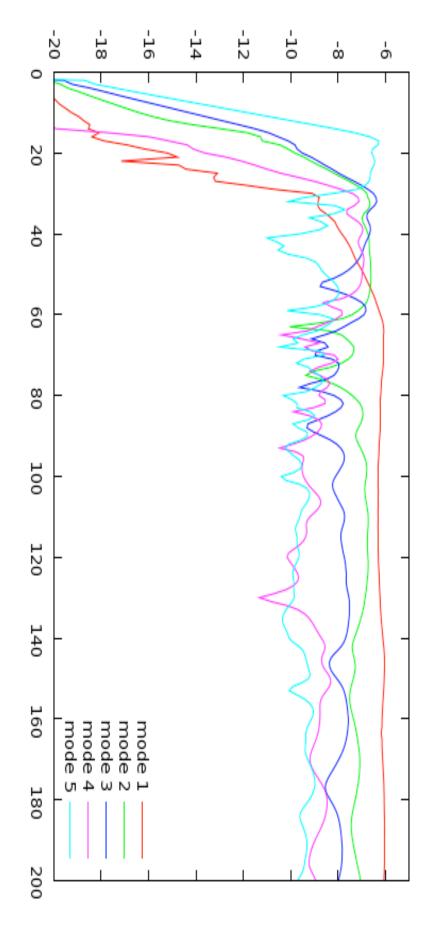
Rossby wave Instability: 3D evolution

-Growth of vortices with spiral waves Initial condition : background equilibrium + gaussian bump in density and pressure + small perturbation



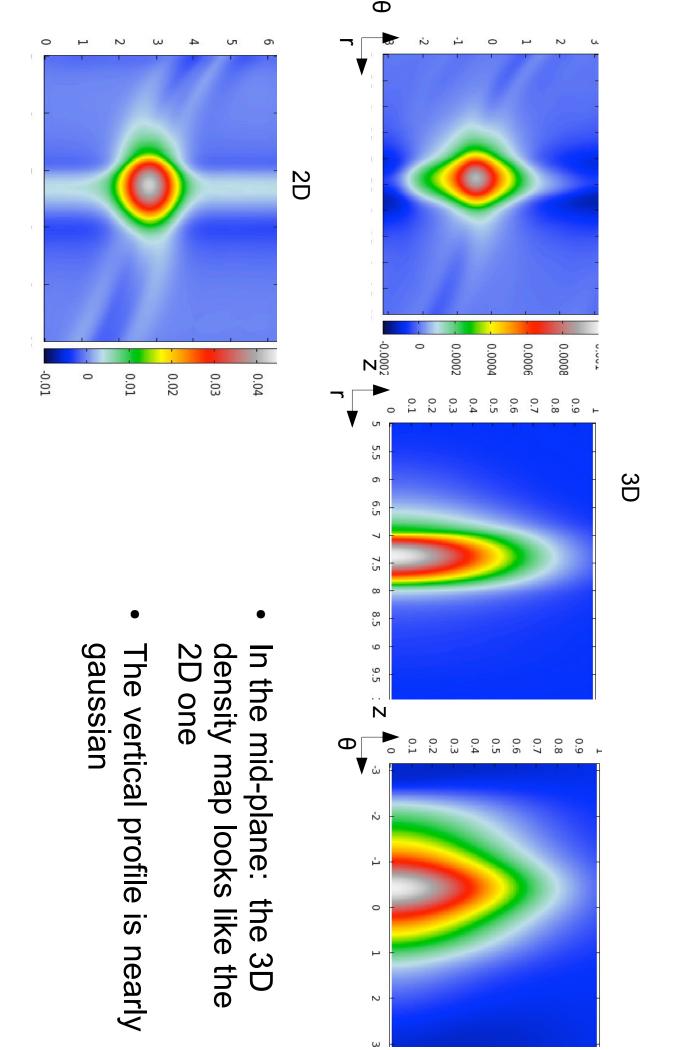
- Gradual merging of the vortices (mode number decreases)
- At the end: a single quasi-steady vortex that migrates toward the center in a slow time scale

Grow of the instability

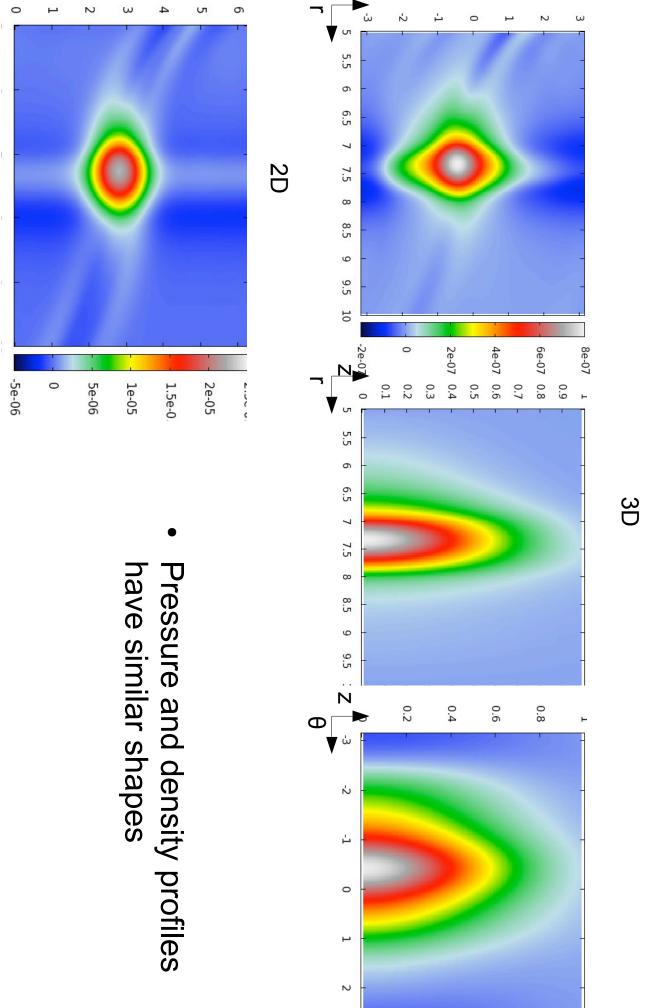


- Beginning is dominate by high mode
- Dominant mode decrease until the mode 1 is the dominant
- Amplitude of mode 1 doesn't decrease after saturation

Density once a single vortex is formed



Pressure profile



Vertical equilibrium

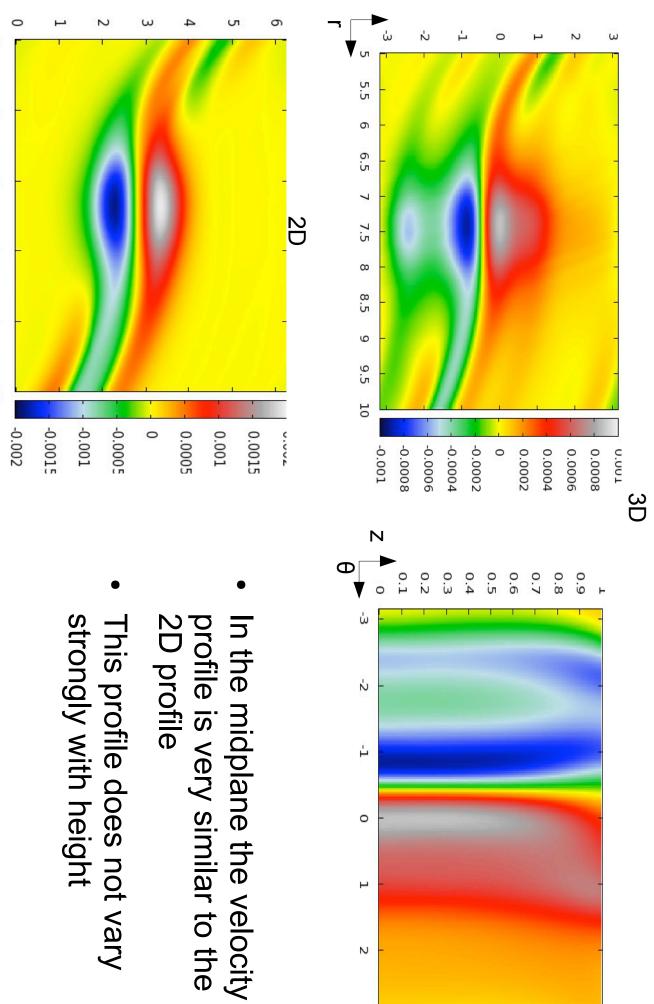
Pressure and density have similar profile, so temperature is not modified

Vertical hydrostatic equilibrium reads :



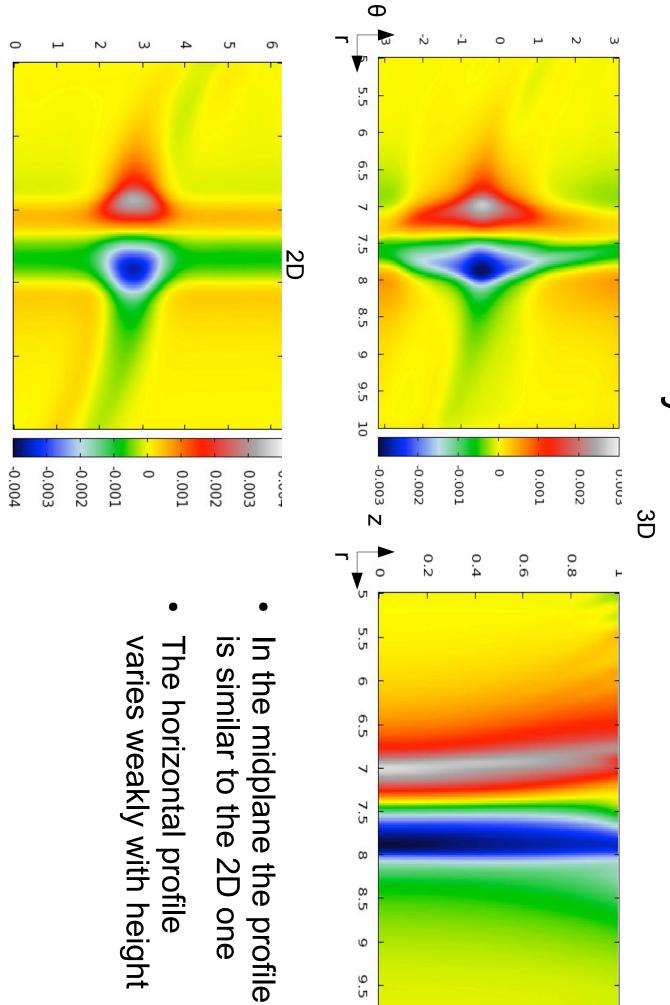
As temperature doesn't change, the vertical equilibrium is not modified

Radial velocity

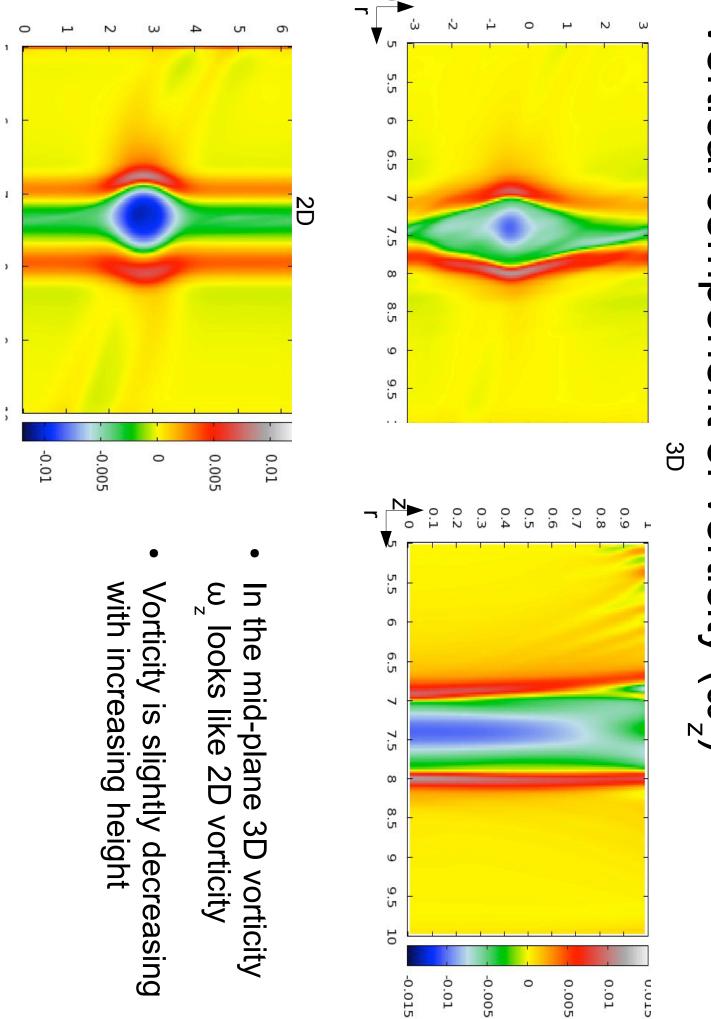


Φ

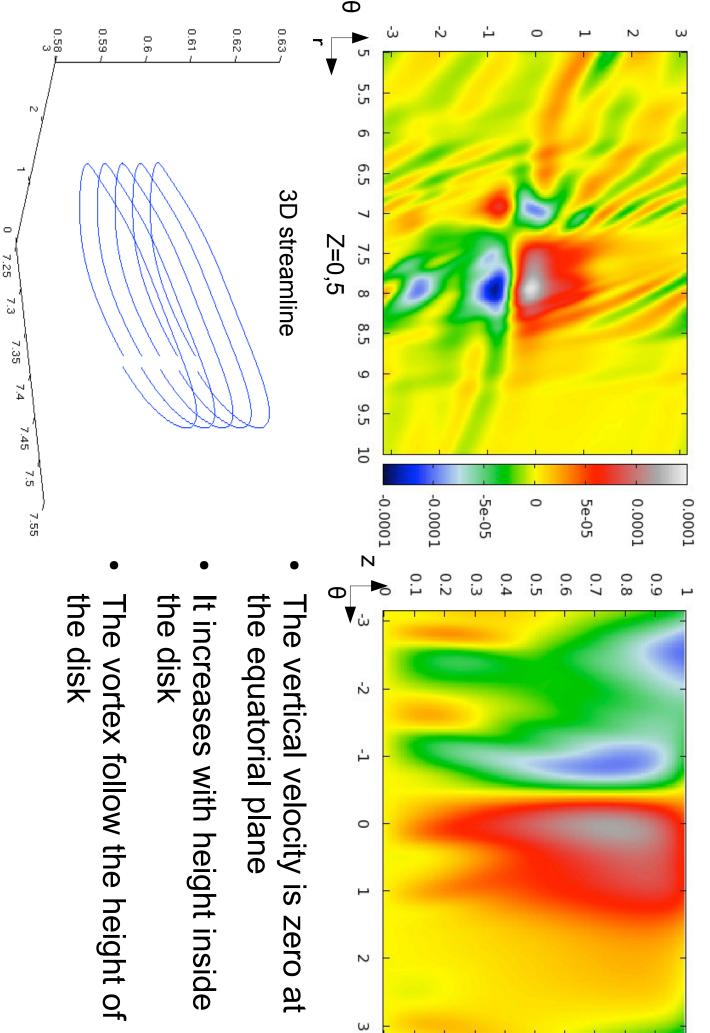
Azimuthal velocity



Vertical component of vorticity (ω_z)



Vertical velocity



Vertical velocity

The vertical velocity comes from the entropy gradient of the disk:

In the rotating frame, the entropy equation is:



If Ω_0 is the angular velocity of the vortex, the flow is stationary so

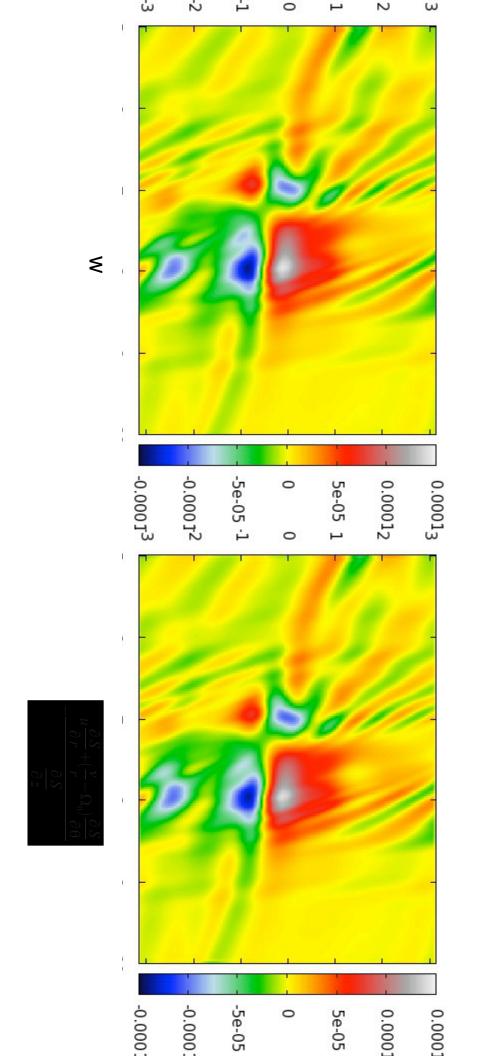


(i.e) fluid particles stay on surfaces of constant entropy

The vertical velocity reads also :



Vertical velocity



we check with the numerical values and found good agreement

Role of stratification

The vertical stratification is given by the Brunt-Väisälä frequency:



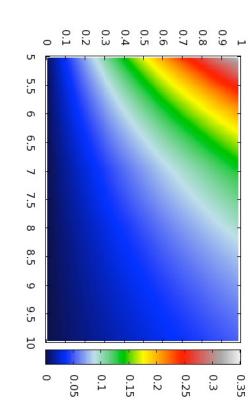
- N²>0 the stratification is stable : when a fluid particle change its altitude, a restoring force appears
- altitude, a force which will amplify the motion will appears N²<0 the stratification is unstable : when a fluid particle change its

Stratification

Brunt Väisälä in our case

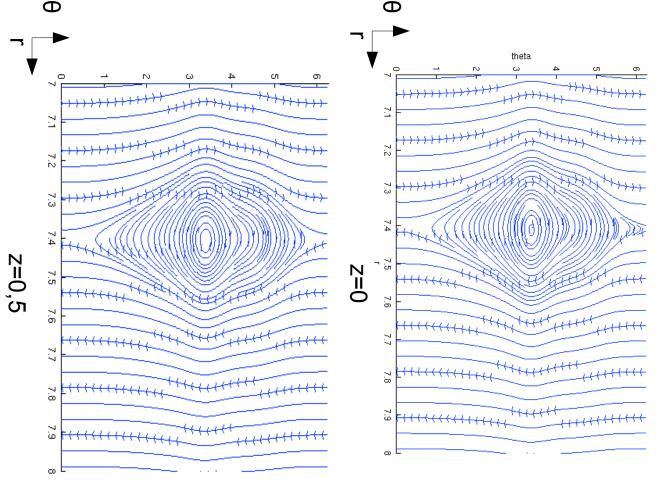
Always positive :

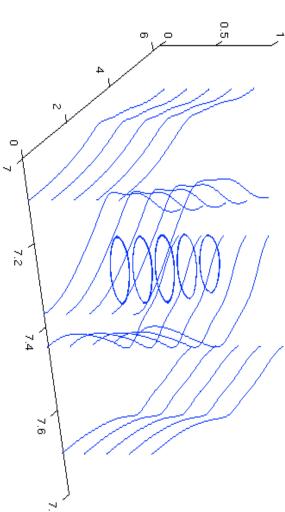
stable vertical stratification



Fluid particle can't move vertically without be affected by a restoring force, it's why vertical motions are small

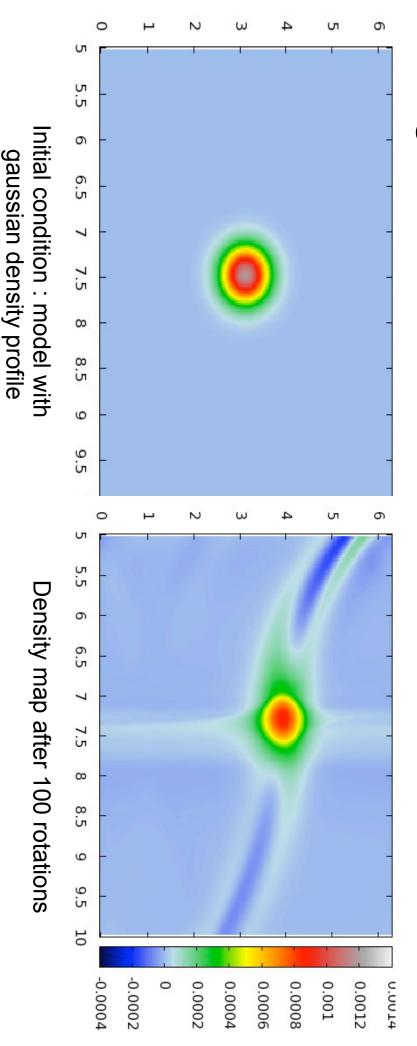
Streamline in the rotating trame





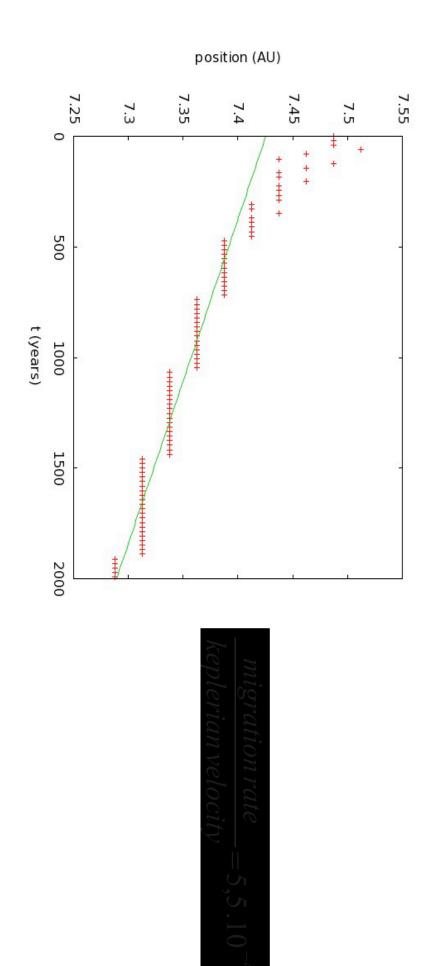
- The streamline are plotted in the rotating frame, when the flow is steady, so the streamline coincide with the trajectory of fluid particles
- The rotation of the gas is mainly in the horizontal plane
- Columnar anticyclonic vortices

Long time evolution



- We start from a vortex model to study its long time evolution
- survives more than 100 rotation periods After a few rotations, it relaxes to a quasi stationary vortex that
- Rossby wave instability The structure of the vortex looks like the vortex obtained by the

Migration of the vortex



- After the relaxation phase, the migration rate is constant like in 2D
- rotations (consistent with the 2D result) The migration rate 6,8.10⁻² AU / 1000 years or 0,126 AU/ 100

Conclusion

- We confirm that Rossby instability occurs in 3D as in 2D.
- slowly migrate toward the central star Formed vortices are columnar quasi-steady structures that
- A simple vortex model obtained as an approximate solution of the steady state fluid equations is found to relaxes to such vortices